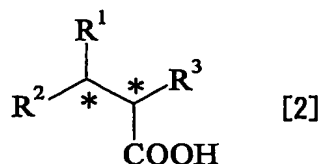
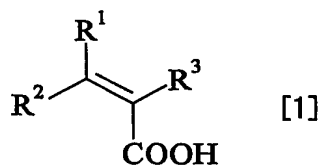


claim

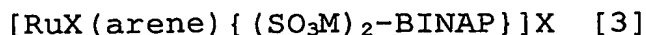
1. A method for producing an optically active carboxylic acid represented by the formula [2]:



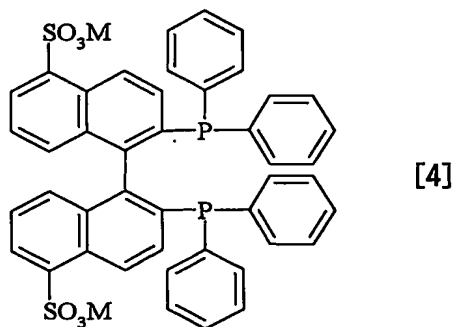
wherein  $R^1$ ,  $R^2$  and  $R^3$  independently represent a hydrogen atom, an alkyl group, an alkenyl group or an aryl group, the groups may have a substituent,  $R^1$ ,  $R^2$  and  $R^3$  is not a hydrogen atom simultaneously,  $R^3$  is a group other than a hydrogen atom when one of  $R^1$  and  $R^2$  is a hydrogen atom,  $R^3$  is a group other than a hydrogen atom and a methyl group when both of  $R^1$  and  $R^2$  are hydrogen atoms, and  $R^1$  and  $R^2$  are different groups other than a hydrogen atom when  $R^3$  is a hydrogen atom, and at least one of the two carbon atoms marked with \* represents an asymmetric carbon atom, comprising the step of subjecting an  $\alpha,\beta$ -unsaturated carboxylic acid represented by the formula [1]:



wherein  $R^1$  to  $R^3$  have the same meanings as those in the formula [2], in the presence of a sulfonated BINAP-Ru complex represented by the formula [3]:



wherein  $(\text{SO}_3\text{M})_2\text{-BINAP}$  represents a tertiary phosphine represented by the formula [4]:



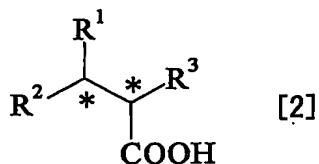
M represents an alkaline metal atom, X represents a chlorine atom, a bromine atom or an iodine atom, and arene represents a benzene or an alkyl-substituted benzene, in an aqueous solvent, to an asymmetric hydrogenation.

2. The method according to claim 1, wherein the aqueous solvent is water or a mixed solvent of water and a water-insoluble organic solvent.

3. The method according to claim 1, wherein the sulfonated BINAP-Ru complex is recovered.

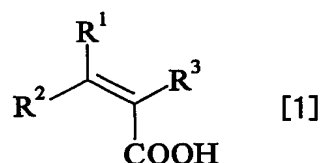
4. The method according to claim 1, wherein the sulfonated BINAP-Ru complex is recycled.

5. A method for producing an optically active carboxylic acid represented by the formula [2]:



wherein  $\text{R}^1$ ,  $\text{R}^2$  and  $\text{R}^3$  independently represent a hydrogen atom,

an alkyl group, an alkenyl group or an aryl group, the groups may have a substituent,  $R^1$ ,  $R^2$  and  $R^3$  is not a hydrogen atom simultaneously,  $R^3$  is a group other than a hydrogen atom when one of  $R^1$  and  $R^2$  is a hydrogen atom,  $R^3$  is a group other than a hydrogen atom and a methyl group when both of  $R^1$  and  $R^2$  are hydrogen atoms, and  $R^1$  and  $R^2$  are different groups other than a hydrogen atom when  $R^3$  is a hydrogen atom, and at least one of the two carbon atoms marked with \* represents an asymmetric carbon atom, comprising the step of subjecting an  $\alpha,\beta$ -unsaturated carboxylic acid represented by the formula [1]:



wherein  $R^1$  to  $R^3$  have the same meanings as those described above, in the presence of a recovered sulfonated BINAP-Ru complex used in the method according to claim 1 in water or a mixed solvent of water and a water-insoluble organic solvent to an asymmetric hydrogenation.

6. The method according to claim 5, wherein the  $\alpha,\beta$ -unsaturated carboxylic acid is hydrogenated in the presence of an aqueous solution containing the sulfonated BINAP-Ru complex, and the aqueous solution is obtained by separating a water phase from the reaction mixture after the asymmetric hydrogenation in the method according to claim 1.